

**SPICE Model Formulas**

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**11/26/91**

Diode:

```
.model _name d()
```

Pick two points on Vd - Id curve at low Id, one at highest Id.

$$N = \frac{38.5(Vd1 - Vd2)}{\ln(Id1 / Id2)}$$

$$IS = Id1 \exp[-38.5(Vd1) / N]$$

$$RS = \frac{Vd3 - [(N / 38.5) \ln(Id3 / IS)]}{Id3}$$

Use reverse recovery time info. Ir is negative.

$$TT = \frac{trr}{\ln[(If - Ir) / -Ir]}$$

Pick three points on Cd - Vd curve. One at V = 0, one at low V, one at high V. Start with VJ = 0.5, then iterate M and VJ. Vd is negative.

$$CJO = Cdo$$

$$M = \frac{\ln(C2 / C3)}{\ln[(VJ - Vd3) / (VJ - Vd2)]}$$

$$VJ = \frac{Vd2}{1 - [CJO / C2]^{(1 / M)}}$$

$$EG = \begin{matrix} 1.11 & Si \\ 0.69 & Schottky \\ 0.67 & Ge \end{matrix}$$

$$XTI = \begin{matrix} 3.0 & p-n \\ 2.0 & Schottky \end{matrix}$$

Use breakdown voltage and leakage currents. Vbr is negative.

$$BV = -Vbr$$

$$IBV = Ir \quad \text{leakage current at 80\% or more of breakdown}$$

Zener:

Subcircuit. Uses two diode, one voltage source.

```
.subckt _1n751 1 2
Dx 1 3 z$dx
Vx 3 2 dc 4.00
Dy 2 1 z$dy
.model z$dy d(
+           n = 1.17
+           is = 3.7e-14
+           rs = 1.1
+           cjo = 160e-12
+           m = 0.66
+           vj = 0.78
+           bv = 8.2
+           ibv = 80e-6
+           )
.model z$dx d(rs = 17)
.ends _1n751
```

DY diode is made as a normal diode except for breakdown.

BV = 1.6 Vz

IBV = 2 Ir leakage at 80% of breakdown

DX, VX, use zener current and impedance.

RS = Rz

VX = Vz -  $\frac{[\ln(Iz / 10e-14) + 1]}{38.5} - Rz(Iz - Ir)$

38.5

BJT:

|  |
|--|
| <pre>.model _name npn() .model _name pnp()</pre> |
|--|

$$BF = H_{femax}$$

Pick two points on  $V_{be} - I_c$  curve at low  $I_c$ .

$$NF = \frac{38.5(V_{be2} - V_{be1})}{\ln(I_{c2}/I_{c1})}$$

$$IS = I_{c1} \exp[-38.5(V_{be1}/NF)]$$

Pick two points on  $V_{besat}, V_{cesat} - I_c$  curves. One at low  $I_c$ , one at max  $I_c$ .  $I_c/I_b$  is usually 10.

$$RB = \frac{V_{besat} - (NF/38.5) \ln(I_c/IS)}{I_b}$$

$$RC = \frac{V_{cesatmax} - V_{cesatmin}}{I_c}$$

$$NR = NF$$

$$BR = \frac{IS \{ \exp[38.5(V_{besatmin} - V_{cesatmin})/NR] \}}{I_b - (IS/BF) \{ \exp[38.5(V_{besatmin}/NF)] \}}$$

Pick two point on  $V_{ce} - I_c$  graph at higher  $I_c$ . Else use hoe.

$$VAF = \frac{I_{c1}(V_{ce2} - V_{ce1}) - V_{ce1}}{I_{c2} - I_{c1}}$$

$$VAF = I_c/hoe - V_{ce}$$

Find  $I_c$  at intersection of upper asymptote on  $H_{fe} - I_c$  curve. Pick two points on lower asymptote.  $I_1$  is at intersection of lower asymptote.

$$IKF = I_c \text{ at intersection}$$

$$NE = \frac{NF}{\frac{1 - \ln(BF) - \ln(h_{fe2})}{\ln(I_1) - \ln(I_{c2})}}$$

$$ISE = (IS/BF) \{ I_1/IS \}^{(1 - 1/NE)}$$

Pick three points on C - V curves. One at  $V_r = 0$ , one at low  $V_r$ , and one at high  $V_r$ . Start with a guess of  $VJ_x = 0.5$  and  $MJ_x = 0.3$ , then iterate. Note  $Vr_x$  is negative. If capacitance at  $V_r = 0$  is unknown, then use:

$$CJ_x = C[1 - V_r/VJ_x]^{-MJ_x}$$

$$CJC = C_{c0} \text{ or } C_{cb} \text{ at } V_r = 0$$

$$MJC = \frac{\ln(C1/C2)}{\ln[(VJ - Vr1)/(VJ - Vr2)]}$$

$$VJC = \frac{Vr1}{1 - [CJC/C1]^{(1/MJC)}}$$

$$XCJC = 0.8$$

$$CJE = C_{c0} \text{ or } C_{cb} \text{ at } V_r = 0$$

$$MJE = \text{similar to } MJC$$

$$VJE = \text{similar to } VJC$$

$$CJS = C_{cs} \text{ collector to substrate}$$

$$MJS = \text{similar to } MJC$$

$$VJS = \text{similar to } VJC$$

Pick two points on  $f_t - I_c$  curve, one at max, and the intersection of the asymptote for high  $I_c$  rolloff. Leave VTF at infinity.

$$TF = \frac{1}{2(\pi)ft_{max}}$$

$$XTF = 4$$

$$ITF = I_c \text{ at upper asymptote.}$$

Use storage time data. If forward and reverse currents are unknown, use second equation.

$$TR = \frac{ts}{BR \ln[(I_{bf} + I_{br})/(I_c/BF + I_{br})]}$$

$$TR = \frac{2 ts}{BR}$$

JFET:

```
.model _name njf()  
.model _name pjf()
```

Use  $V_{gsoff}$  or  $V_{gs} - I_d$  curve.  $V_{gs}$  may be negative. Also  $I_{dss}$ .

$$VTO = V_{gsoff}$$

$$BETA = \frac{I_{dss}}{VTO^2}$$

$$BETA = \frac{y_{fs}}{2[1 + LAMBDA(V_{ds})][V_{gs} - VTO]}$$

$$BETA = \frac{I_d}{2(V_{ds})[V_{gs} - VTO] - V_{ds}^2}$$

Use  $y_{os}$  data.

$$LAMBDA = \frac{y_{os}}{BETA(VTO^2)}$$

Pick two points on  $y_{fs} - I_d$  curve, one at high  $I_d$ , one at low  $I_d$ .

$$RS = \frac{y_{fs1}[\ln(I_{d2})/\ln(I_{d1})]}{y_{fs2}\{y_{fs1}[\ln(I_{d2})/\ln(I_{d1})] + 1\}}$$

Use capacitance data at  $V_r = 0$ .

$$CGS = C_{gso}$$

$$CGD = C_{gdo}$$

$$PB = \frac{V_{gs} - V_{ds}}{1 - [CGD/C_{ds}]^2}$$

MOSFET:

```
.model _name nmos()
.model _name pmos()
```

Use  $V_{gsoff} - I_d$  curve. Note  $V_{gs}$  may be negative.  $V_{bs}$  is negative.

$$V_{TO} = V_{gsoff} \text{ at } V_{bs} = 0$$

$$PHI = 0.6$$

Use  $V_{gsoff} - V_{bs}$  curve.

$$GAMMA = \frac{V_{gsoff} - V_{TO}}{[PHI - V_{bs}]^{0.5} - [PHI]^{0.5}}$$

Use  $V_{gs} - I_d$  curve. Pick a point at high  $I_d$ .

$$KP = \frac{2 I_d}{[V_{gs} - V_{TO}]^2}$$

Pick two points on  $V_{ds} - I_d$  curve at high  $I_d$ .

$$LAMBDA = \frac{I_{d2} - I_{d1}}{(I_{d1})(V_{ds2}) - (I_{d2})(V_{ds1})}$$

$$LAMBDA = \frac{g_{os}}{I_d}$$

Pick two points on  $g_{fs} - I_d$  graph, one at high  $I_d$ , one at low  $I_d$ .

$$RS = \frac{(g_{fs1}) \ln(I_{d2}/I_{d1})}{2(G_{fs2}) [(g_{fs1}) \ln(I_{d2}/I_{d1}) + 1]}$$

$$RD = RS$$